

# CS450

## Structure of Higher Level Languages

Lecture 29: Refactoring errors; monads

Tiago Cogumbreiro

# Today we will learn about...

- Errors in our interpreter: user errors versus implementation errors
- Handling implementation errors
- Refactoring our interpreter
- Handling errors with a monadic interface
- Monadic list comprehension

# Error handling

# Recall our interpreter from HW3

```

(define (r:eval-builtin sym)
  (cond [(equal? sym '+) +]
        [(equal? sym '*) *]
        [(equal? sym '-') -]
        [(equal? sym '/') /]
        [else #f]))

(define (r:eval-exp exp)
  (cond
    [(r:number? exp) (r:number-value exp)]
    [(r:variable? exp) (r:eval-builtin (r:variable-name exp))]
    [(r:apply? exp)
     ((r:eval-exp (r:apply-func exp))
      (r:eval-exp (first (r:apply-args exp)))
      (r:eval-exp (second (r:apply-args exp))))])
    [else (error "Unknown expression:" exp)]))
  
```

# Consider the following example

What happens if we run this example?

```
(r:eval-exp 10)
```

# Consider the following example

What happens if we run this example?

```
(r:eval-exp 10)
; Unknown expression: 10
; context...:
```

The caller should be passing an AST, not a number!

We should be using contracts to avoid this kind of error!

# Consider the following example

What happens if the user tries to divide a number by zero?

```
(r:eval-exp (r:apply (r:variable '/') (list (r:number 1) (r:number 0))))
```

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What happens if the user tries to divide a number by zero?

```
(r:eval-exp (r:apply (r:variable '/') (list (r:number 1) (r:number 0))))
; /: division by zero
; context...:
```

Is this considered an error?



# How can we solve this problem?

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■ Is this a user error? Or is this an implementation error?

Is it an implementation problem?

■ **Implementation errors should be loud!** We want our code to crash during testing. This family of errors could correspond to a bug, or, more importantly, to a misunderstanding between the developer and the client! Using the exceptions model of our client is a big plus, as we get stack trace information, among other niceties.

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What does the error mean?

■ Is this a user error? Or is this an implementation error?

Is it an implementation problem?

■ **Implementation errors should be loud!** We want our code to crash during testing. This family of errors could correspond to a bug, or, more importantly, to a misunderstanding between the developer and the client! Using the exceptions model of our client is a big plus, as we get stack trace information, among other niceties.

Is it a user error?

■ User errors must be handled **gracefully** and **cannot** crash our application. User errors must also not reveal the internal state of the code (**no stack traces!**), as such information can pose a security threat.

# Handling run-time errors

# Solving the division-by-zero error

1. We can implement a safe-division that returns a special return value
2. We can let Racket crash and catch the exception

# Implementing safe division

- Implement a safe-division that returns a special return value

# Implementing safe division

Implement a safe-division that returns a special return value

```
(define (safe-/ x y)
  (cond [(= y 0) #f]
        [else (/ x y)]))
```



# Is this enough?

# Is this enough?

```

(r:eval-exp
  (r:apply
    (r:variable '+)
    (list
      (r:apply (r:variable '/') (list (r:number 1) (r:number 0)))
      (r:number 10))))
; +: contract violation
;   expected: number?
;   given: #f
;   argument position: 1st
;   [,bt for context]
  
```

We still need to rewrite `r:eval-exp` to handle `#f`

# Solving apply

■ (Demo...)

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(Demo...)

```
(define (r:eval-exp exp)
  (cond
    [(r:number? exp) (r:number-value exp)]
    [(r:variable? exp) (r:eval-builtin (r:variable-name exp))]
    [(r:apply? exp)
     (define arg1 (r:eval-exp (first (r:apply-args exp))))
     (cond
       [(false? arg1) arg1]
       [else
        (define arg2 (r:eval-exp (second (r:apply-args exp))))
        (cond
          [(false? arg2) arg2]
          [else ((r:eval-exp (r:apply-func exp)) arg1 arg2)])])]
    [else (error "Unknown expression:" exp)]))
```

# Error handling API

# How can we abstract this pattern?

```

(define arg1 (r:eval-exp (first (r:apply-args exp))))
(cond
  [(false? arg1) arg1]
  [else
   (define arg2 (r:eval-exp (second (r:apply-args exp))))
   (cond
     [(false? arg2) arg2]
     [else ((r:eval-exp (r:apply-func exp)) arg1 arg2)])])
  
```

# How can we abstract this pattern?

```

(define arg1 (r:eval-exp (first (r:apply-args exp))))
(cond
  [(false? arg1) arg1]
  [else
   (define arg2 (r:eval-exp (second (r:apply-args exp))))
   (cond
     [(false? arg2) arg2]
     [else ((r:eval-exp (r:apply-func exp)) arg1 arg2)])])
  
```

## Refactoring

```

(define (handle-err res kont)
  (cond
    [(false? res) res]
    [else (kont res)]))
  
```

# Rewriting our code with `handle-err`

(Demo...)



# Rewriting our code with `handle-err`

(Demo...)

```
(handle-err (r:eval-exp (first (r:apply-args exp))))  
  (lambda (arg1)  
    (handle-err (r:eval-exp (second (r:apply-args exp))))  
      (lambda (arg2)  
        ((r:eval-exp (r:apply-func exp)) arg1 arg2))))))
```

# Example 3

```

(r:eval-exp (r:apply (r:variable 'modulo) (list (r:number 1) (r:number 0))))
; application: not a procedure;
; expected a procedure that can be applied to arguments
; given: #f
; [,bt for context]

```

# Let us revisit `r:eval`

(Demo...)

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(Demo...)

```
(handle-err (r:eval-exp (r:apply-func exp))
  (lambda (func)
    (handle-err (r:eval-exp (first (r:apply-args exp)))
      (lambda (arg1)
        (handle-err (r:eval-exp (second (r:apply-args exp)))
          (lambda (arg2)
            (func arg1 arg2))))))))))
```

Where have we seen this before?

# Let us revisit `r:eval`

(Demo...)

```
(handle-err (r:eval-exp (r:apply-func exp))
  (lambda (func)
    (handle-err (r:eval-exp (first (r:apply-args exp)))
      (lambda (arg1)
        (handle-err (r:eval-exp (second (r:apply-args exp)))
          (lambda (arg2)
            (func arg1 arg2))))))))))
```

Where have we seen this before?

Monads!

# Handling errors with monads

# Monads

A general functional pattern that abstracts **assignment** and **control flow**

- Monads are not just for handling state
- Monads were introduced in Haskell by Philip Wadler in 1990

## The monadic interface

- **Bind:** combines two effectful operations  $o_1$  and  $o_2$ . Operation  $o_1$  produces a value that is consumed by operation  $o_2$ .

```
(define (handle-err res kont) (cond [(false? res) res] [else (kont res)])) ; For err
```

- **Pure:** Converts a pure value to a monadic operation, which can then be chained with bind.

```
(define (pure e) e) ; For err
```

# Re-implementing the do-notation

Let us copy-paste our macro and replace `bind` by `handle-err`.

```
(define-syntax do
  (syntax-rules (←)
    ; Only one monadic-op, return it
    [(_ mexp) mexp]
    ; A binding operation
    [(_ var ← mexp rest ...) (handle-err mexp (lambda (var) (do rest ...)))]
    ; No binding operator, just ignore the return value
    [(_ mexp rest ...) (handle-err mexp (lambda (-) (do rest ...)))]))
```



# Rewriting `r:eval-builtin`

(Demo...)

# Rewriting r:eval-builtin

(Demo...)

```
(do
  func ← (r:eval-exp (r:apply-func exp))
  arg1 ← (r:eval-exp (first (r:apply-args exp)))
  arg2 ← (r:eval-exp (second (r:apply-args exp)))
  (func arg1 arg2))
```

# Monadic List Comprehension

# Monad: List comprehension

List comprehension is a mathematical notation to succinctly describe the members of the list.

$$[(x, y) \mid x \leftarrow [1, 2]; y \leftarrow [3, 4]] = [(1, 3), (1, 4), (2, 3), (2, 4)]$$

```
(define lst
  (do
    x ← (list 1 2)
    y ← (list 3 4)
    (list-pure (cons x y))))
; Result
(check-equal? lst (list (cons 1 3) (cons 1 4) (cons 2 3) (cons 2 4)))
```

# Designing the list monad

## The join operation

Spec

```
(check-equal? (join (list (list 1 2)))  
              (list 1 2))  
(check-equal? (join (list (list 1) (list 2)))  
              (list 1 2))  
(check-equal? (join (list (list 1 2) (list 3)))  
              (list 1 2 3))
```

# Designing the list monad

## The join operation

### Spec

```
(check-equal? (join (list (list 1 2)))  
              (list 1 2))  
(check-equal? (join (list (list 1) (list 2)))  
              (list 1 2))  
(check-equal? (join (list (list 1 2) (list 3)))  
              (list 1 2 3))
```

### Solution

```
(define (join elems)  
  (foldr append empty elems))
```

# Designing the list monad

```
(define (list-pure x) (list x))
```

```
(define (list-bind op1 op2)  
  (join (map op2 op1)))
```

# Re-implementing the do-notation

Let us copy-paste our macro and replace `bind` by `list-bind`.

```
(define-syntax do
  (syntax-rules (←)
    ; Only one monadic-op, return it
    [(_ mexp) mexp]
    ; A binding operation
    [(_ var ← mexp rest ...) (list-bind mexp (lambda (var) (do rest ...)))]
    ; No binding operator, just ignore the return value
    [(_ mexp rest ...) (list-bind mexp (lambda (_) (do rest ...)))]))
```



# Desugaring list comprehension

```

(define lst
  (do
    x ← (list 1 2)
    y ← (list 3 4)
    (pure (cons x y))))
; =
(define lst
  (list-bind (list 1 2)
    (lambda (x)
      (list-bind (list 3 4)
        (lambda (y)
          (list-pure (cons x y))))))))

```

```
(join
  (map
    (lambda (x)
      (join (map (lambda (y) (list (cons x y))) (list 3 4))))
    (list 1 2)))
; =
(join
  (map
    (lambda (x) (join (list (list (cons x 3)) (list (cons x 4))))
      (list 1 2)))
; =
(join
  (map
    (lambda (x) (list (cons x 3) (cons x 4)))
    (list 1 2)))
; =
(join (list (list (cons 1 3) (cons 1 4)) (list (cons 2 3) (cons 2 4))))
; =
(list (cons 1 3) (cons 1 4) (cons 2 3) (cons 2 4))
```

# Examples

## Example 1

```
(check-equal? (list-bind (lambda (x) (list x x)) (list 1 2 3))
```

# Examples

## Example 1

```
(check-equal? (list-bind (lambda (x) (list x x)) (list 1 2 3))  
              (list 1 1 2 2 3 3))
```

## Example 2

```
(check-equal? (do x ← (list 1 2) (list (* x 10) (+ x 2) (- x 1)))
```

# Examples

## Example 1

```
(check-equal? (list-bind (lambda (x) (list x x)) (list 1 2 3))  
              (list 1 1 2 2 3 3))
```

## Example 2

```
(check-equal? (do x ← (list 1 2) (list (* x 10) (+ x 2) (- x 1)))  
              (list 10 3 0 20 4 1))
```

## Example 3

```
(check-equal? (list-bind (lambda (x) (list))) (list 1 2 3))
```

# Examples

## Example 1

```
(check-equal? (list-bind (lambda (x) (list x x)) (list 1 2 3))
              (list 1 1 2 2 3 3))
```

## Example 2

```
(check-equal? (do x ← (list 1 2) (list (* x 10) (+ x 2) (- x 1)))
              (list 10 3 0 20 4 1))
```

## Example 3

```
(check-equal? (list-bind (lambda (x) (list))) (list 1 2 3))
              (list))
```

# Examples

## Example 4

```
(check-equal? (do x ← (list 1 2 3 4) (if (even? x) (pure x) empty))
```

# Examples

## Example 4

```
(check-equal? (do x ← (list 1 2 3 4) (if (even? x) (pure x) empty))
              (list 1 3))
```

$$[x \mid x \leftarrow [1, 2, 3, 4] \text{ if even?}(x)] = [1, 3]$$