

CS450

Structure of Higher Level Languages

Lecture 13: Shared mutable state and immutability

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Policy on academic honesty

1. Any two students sharing code in a submission **will void both submissions**.
2. Any repeated incident will be reported to the department, and the student **will fail the course with an F**.

Students may choose to withdraw any homework submission that has not been voided.

Please read on...

[Acknowledging Intellectual Debts](#). [Nurit Haspel](#), [Ethan Bolker](#), [Carl Offner](#).

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Anti-Cheating Software



Moss Results

Thu Mar 21 09:40:13 PDT 2019

Options -l scheme -m 10

Scheme files

[[How to Read the Results](#) | [Tips](#) | [FAQ](#) | [Contact](#) | [Submission Scripts](#) | [Credits](#)]

File 1	File 2	Lines Matched
assignment_154296_export/submission	.rkt (58%) assignment_154296_export/submission	.rkt (60%) 97
assignment_154296_export/submission	.rkt (52%) assignment_154296_export/submission	.rkt (51%) 85
assignment_154296_export/submission	.rkt (50%) assignment_154296_export/submission	.rkt (47%) 74
assignment_154296_export/submission	.rkt (99%) assignment_154296_export/submission	.rkt (99%) 113
assignment_154296_export/submission	.rkt (24%) assignment_154296_export/submission	.rkt (34%) 66
assignment_154296_export/submission	.rkt (32%) assignment_154296_export/submission	.rkt (39%) 45
assignment_154296_export/submission	.rkt (20%) assignment_154296_export/submission	.rkt (29%) 61
assignment_154296_export/submission	.rkt (20%) assignment_154296_export/submission	.rkt (30%) 61
assignment_154296_export/submission	.rkt (28%) assignment_154296_export/submission	.rkt (35%) 35
assignment_154296_export/submission	.rkt (27%) assignment_154296_export/submission	.rkt (35%) 33

Cheating sample

assignment_154296_export/submission_ [REDACTED].rkt (99%)	[REDACTED]	assignment_ [REDACTED] _export/submissio (99%)
2-114	[REDACTED]	2-108

assignment_154296_export/submission_ .rkt

```
#lang racket
[REDACTED]

(require "ast.rkt")
(require "hw1.rkt")
(require rackunit)
(provide (all-defined-out))

;use if for number 1
;

;; Exercise 1.a: Read-write cell
;; Solution has 3 lines.
(define (rw-cell x)
  ((lambda (a)
     (lambda (b) (if (equal? 1 (length b))
                     (rw-cell (car b))
                     a)))
     x))

;; Exercise 1.b: Read-only cell
;; Solution has 4 lines.
(define (ro-cell x)
  ((lambda (a)
     (lambda (b) (if (equal? 1 (length b))
                     (ro-cell a)
                     a))))
     x))
```

assignment_154296_export/submission_ .rkt

```
#lang racket
[REDACTED]

(require "ast.rkt")
(require "hw1.rkt")
(require rackunit)
(provide (all-defined-out))

;; Exercise 1.a: Read-write cell
;; Solution has 3 lines.
(define (rw-cell x)
  ((lambda (a)
     (lambda (b) (if (equal? 1 (length b))
                     (rw-cell (car b))
                     a)))
     x))

;; Exercise 1.b: Read-only cell
;; Solution has 4 lines.
(define (ro-cell x)
  ((lambda (a)
     (lambda (b) (if (equal? 1 (length b))
                     (ro-cell a)
                     a))))
     x))
```

Today we will...

1. Study adding **define** to our language
2. Introduce mutation in an immutable setting
3. Introduce Racket's contracts

λ_D -calculus: λ -calculus with definitions

Syntax

$$t ::= e \mid t; t \mid (\text{define } x \ e)$$

$$e ::= v \mid x \mid (e_1 \ e_2) \mid \lambda x. t \quad v ::= n \mid (E, \lambda x. t) \mid \text{void}$$

- New grammar rule: *terms*
- A program is now a non-empty sequence of terms
- Since we are describing the *abstract* syntax, there is no distinction between a basic and a function definition
- Since evaluating a definition returns a void, we need to update values

Values

■ We add `void` to values.

$$v ::= n \mid (E, \lambda x.t) \mid \mathbf{void}$$

Racket implementation

```
;; Values
(define (s:value? v) (or (s:number? v) (s:closure? v) (s:void? v)))
(struct s:number (value) #:transparent)
(struct s:closure (env decl) #:transparent)
(struct s:void () #:transparent)
```

Expressions

Expressions remain unchanged.

$$e ::= v \mid x \mid (e_1 e_2) \mid \lambda x.t$$

Racket implementation

```
(define (s:expression? e) (or (s:value? e) (s:variable? e) (s:apply? e) (s:lambda? e)))  
(struct s:variable (name) #:transparent)  
(struct s:apply (func args) #:transparent)  
(struct s:lambda (params body) #:transparent)
```


Terms

■ We implement terms below.

$$t ::= e \mid t; t \mid (\mathbf{define} \ x \ e)$$

Racket implementation

```
(define (s:term? t) (or (s:expression? t) (s:seq? t) (s:define? t)))
(struct s:seq (fst snd) #:transparent)
(struct s:define (var body) #:transparent)
```

The body of a function declaration is a single term

The body is no longer a list of terms!

■ A sequence is not present in the concrete syntax, but it simplifies the implementation and formalism (see reduction)

Parsing datum into AST terms

- Our parser handles multiple terms in the body of a function declaration.
- Function `s:parse1` parses a single term.

```
(check-equal?
 (s:parse1 '(lambda (x) x y z))
 (s:lambda (list (s:variable 'x))
  (s:seq (s:variable 'x)
   (s:seq (s:variable 'y) (s:variable 'z))))))
```

Parsing datum into AST terms

The body of a function can have one or more definitions, values, or function calls.

```
(check-equal?
 (s:parse1 '(lambda (x) (define x 3) x))
 (s:lambda (list (s:variable 'x))
  (s:seq (s:define (s:variable 'x) (s:number 3)) (s:variable 'x))))
```

Parsing datum into AST terms

- Parsing supports function definitions.
- Function `s:parse` can parse a sequence of terms, which corresponds to a Racket program.

```
(check-equal?
 (s:parse '[(define (f x) x) (f 1)])
 (s:define (s:variable 'f) (s:lambda (list (s:variable 'x)) (s:variable 'x))))
```

λ_D -calculus: λ -calculus with definitions

Semantics

$$\frac{e \Downarrow_E v}{e \Downarrow_E (E, v)} \quad (\mathbf{E}\text{-exp})$$

$$\frac{e \Downarrow_E v}{(\mathbf{define} \ x \ e) \Downarrow_E (E[x \mapsto v], \mathbf{void})} \quad (\mathbf{E}\text{-def})$$

$$\frac{t_1 \Downarrow_{E_1} (E_2, v_1) \quad t_2 \Downarrow_{E_2} (E_3, v_2)}{t_1; t_2 \Downarrow_{E_1} (E_3, v_2)} \quad (\mathbf{E}\text{-seq})$$

- Evaluating a define *extends* the environment with a new binding
- Sequencing must thread the environments

Please, use your Rule Sheet in the following examples:

$$v \Downarrow_E v \quad (\mathbf{E}\text{-val})$$

$$x \Downarrow_E E(x) \quad (\mathbf{E}\text{-var})$$

$$\lambda x.t \Downarrow_E (E, \lambda x.t) \quad (\mathbf{E}\text{-lam})$$

$$\frac{e_f \Downarrow_E (E_b, \lambda x.t_b) \quad e_a \Downarrow_E v_a \quad t_b \Downarrow_{E_b[x \mapsto v_a]} v_b}{(e_f e_a) \Downarrow v_b} \quad (\mathbf{E}\text{-app})$$

$$\frac{e \Downarrow_E v}{e \Downarrow_E (E, v)} \quad (\mathbf{E}\text{-exp})$$

$$\frac{e \Downarrow_E v}{(\mathbf{define} \ x \ e) \Downarrow_E (E[x \mapsto v], \mathbf{void})} \quad (\mathbf{E}\text{-def})$$

$$\frac{t_1 \Downarrow_{E_1} (E_2, v_1) \quad t_2 \Downarrow_{E_2} (E_3, v_2)}{t_1; t_2 \Downarrow_{E_1} (E_3, v_2)} \quad (\mathbf{E}\text{-seq})$$

Evaluating define

Example 1

Consider the following program

```
(define a 20)
(define b (lambda (x) a))
(b 1)
```

What is the output of this program?

Evaluating define

Example 1

Consider the following program

```
(define a 20)
(define b (lambda (x) a))
(b 1)
```

What is the output of this program? The output is: 20

Let us try and evaluate this program with our λ_D semantics!

Example 1: step 1

Input

```
Environment: []  
Term: (define a 20)
```

Example 1: step 1

Input

```
Environment: []  
Term: (define a 20)
```

Evaluating

Output

```
Environment: [ (a . 20) ]  
Value: #<void>
```

Example 1: step 1

Input

```
Environment: []
Term: (define a 20)
```

Output

```
Environment: [ (a . 20) ]
Value: #<void>
```

Evaluating

$$\frac{20 \Downarrow_{\{\}} 20 \quad (\text{E-val})}{(\text{define } a \ 20) \Downarrow_{\{\}} (\{a : 20\}, \text{void})} \quad \text{E-def}$$

Example 1: step 2

Input

```
Environment: [ (a . 20) ]  
Term: (define b (lambda (y) a))
```

Example 1: step 2

Input

```
Environment: [ (a . 20) ]
Term: (define b (lambda (y) a))
```

Output

```
Environment: [
  (a . 20)
  (b . (closure [(a . 20)] (lambda (y) a)))
]
Expression: #<void>
```

Example 1: step 2

Input

```
Environment: [ (a . 20) ]
Term: (define b (lambda (y) a))
```

Output

```
Environment: [
  (a . 20)
  (b . (closure [(a . 20)] (lambda (y) a)))
]
Expression: #<void>
```

Evaluating

$$\frac{\lambda y.a \Downarrow_{\{a:20\}} (\{a : 20\}, \lambda y.a) \quad (\mathbf{E-lam})}{(\mathbf{define} \ b \ \lambda y.a) \Downarrow_{\{a:20\}} (\{a : 20, b : (\{a : 20\}, \lambda y.a)\}, \mathbf{void})} \quad \mathbf{E-def}$$

Example 1: step 3

Input

```
Environment: [  
  (a . 20)  
  (b . (closure [(a . 20)] (lambda (y) a)))  
]  
Term: (b 1)
```

Example 1: step 3

Input

```
Environment: [
  (a . 20)
  (b . (closure [(a . 20)] (lambda (y) a)))
]
Term: (b 1)
```

Output

```
Environment: [
  (a . 20)
  (b . (closure [(a . 20)] (lambda (y) a)))
]
Expression: 20
```

Evaluation

Example 1: step 3

Input

```
Environment: [
  (a . 20)
  (b . (closure [(a . 20)] (lambda (y) a)))
]
Term: (b 1)
```

Output

```
Environment: [
  (a . 20)
  (b . (closure [(a . 20)] (lambda (y) a)))
]
Expression: 20
```

Evaluation

$$\frac{\frac{\frac{E(b) = (\{a : 20\}, \lambda y.a)}{b \Downarrow_E (\{a : 20\}, \lambda y.a)} \text{E-var} \quad \frac{1 \Downarrow_E 1}{1} \text{E-val} \quad \frac{F(a) = 20}{a \Downarrow_F 20} \text{E-var}}{\frac{(b \ 1) \Downarrow_E 20}{(b \ 1) \Downarrow_E (E, 20)} \text{E-app}}{\text{E-exp}}$$

where

$$E = \{a : 20, b : (\{a : 20\}, \lambda y.a)\}$$

$$F = E[y \mapsto 1] = \{a : 20, b : (\{a : 20\}, \lambda y.a), y : 1\}$$

Evaluating define

Example 2

Consider the following program

```
(define b (lambda (x) a))  
(define a 20)  
(b 1)
```

What is the output of this program?

Evaluating define

Example 2

Consider the following program

```
(define b (lambda (x) a))
(define a 20)
(b 1)
```

What is the output of this program? The output is: 20

Let us try and evaluate this program with our λ_D semantics!

Example 2: step 1

Input

```
Environment: []  
Term: (define b (lambda (y) a))
```

Example 2: step 1

Input

```
Environment: []  
Term: (define b (lambda (y) a))
```

Output

```
Environment: [  
  (b . (closure [] (lambda (y) a))  
)]  
Expression: #<void>
```

Evaluation

Example 2: step 1

Input

```
Environment: []
Term: (define b (lambda (y) a))
```

Output

```
Environment: [
  (b . (closure [] (lambda (y) a)))
]
Expression: #<void>
```

Evaluation

$$\frac{\lambda y.a \Downarrow_{\{\}} (\{\}, \lambda y.a) \quad (\mathbf{E-lam})}{(\mathbf{define} \ b \ \lambda y.a) \Downarrow_{\{\}} (\{b : (\{\}, \lambda y.a)\}, \mathbf{void})} \quad \mathbf{E-def}$$

Example 2: step 2

Input

```
Environment: [  
  (b . (closure [] (lambda (y) a))  
]  
Term: (define a 20)
```

Example 2: step 2

Input

```
Environment: [
  (b . (closure [] (lambda (y) a))
]
Term: (define a 20)
```

Output

```
Environment: [
  (a . 20)
  (b . (closure [] (lambda (y) a))
]
Expression: #<void>
```

Evaluation

Example 2: step 2

Input

```
Environment: [
  (b . (closure [] (lambda (y) a)))
]
Term: (define a 20)
```

Output

```
Environment: [
  (a . 20)
  (b . (closure [] (lambda (y) a)))
]
Expression: #<void>
```

Evaluation

$$\frac{20 \Downarrow_{\{b: (\{\}, \lambda y. a)\}} \quad 20 \quad (\text{E-val})}{(\text{define } a \ 20) \Downarrow_{\{b: (\{\}, \lambda y. a)\}} (\{b : (\{\}, \lambda y. a), a : 20\}, \text{void})} \quad \text{E-def}$$

Example 2: step 3

Input

```
Environment: [  
  (a . 20)  
  (b . (closure [] (lambda (y) a))  
]  
Term: (b 1)
```

Example 2: step 3

Input

```
Environment: [
  (a . 20)
  (b . (closure [] (lambda (y) a)))
]
Term: (b 1)
```

Output

```
Environment: [
  (a . 20)
  (b . (closure [] (lambda (y) a)))
]
Expression: error! a is undefined
```

Insight

When creating a closure we copied the existing environment, and therefore any future updates are forgotten.

The semantics of λ_D is not enough! We need to introduce a notion of **mutation**.

How do implement mutation
without mutable constructs?

Shared "mutable" state
with immutable data-structures

Why, though?

Benefits

- A necessity if we use a language without mutation (such as Haskell)
- Parallelism: A great way to implement fast and safe data-structures in concurrent code (look up copy-on-write)
- Development: Controlled mutation improves code maintainability
- Memory management: counters the problem of circular references (notably, useful in C++ and Rust, see example)

Encoding shared mutable state with immutable data-structures is a great skill to have.

Heap

We want to design a data-structure that represents a *heap* (a shared memory buffer) that allows us to: *allocate* a new memory cell, *load* the contents of a memory cell, and *update* the contents of a memory cell.

Constructors

- `empty-heap` returns an empty heap
- `(heap-alloc h v)` creates a new memory cell in heap `h` whose contents are value `v`
- `(heap-put h r v)` updates the contents of memory handle `r` with value `v` in heap `h`

Selectors

- `(heap-get h r)` returns the contents of memory handle `r` in heap `h`

Heap usage

```
(define h empty-heap) ; h is an empty heap  
(define r (heap-alloc h "foo")) ; stores "foo" in a new memory cell
```

What should the return value of `heap-alloc`?

- Should `heap-alloc` return a copy of `h` extended with "foo"? But then, how do we access the memory cell pointing to "foo"?
- Should `heap-alloc` return a handle to the new memory cell? But, since there is no mutation, how can we access the new heap?

Heap usage

```
(define h empty-heap)           ; h is an empty heap
(define r (heap-alloc h "foo")) ; stores "foo" in a new memory cell
```

What should the return value of `heap-alloc`?

- Should `heap-alloc` return a copy of `h` extended with "foo"? But then, how do we access the memory cell pointing to "foo"?
- Should `heap-alloc` return a handle to the new memory cell? But, since there is no mutation, how can we access the new heap?

Function `heap-alloc` must return a *pair* `eff` that contains the new heap and the memory handle.

```
(struct eff (state result) #:transparent)
```

Heap usage example

Spec

```

(define h1 empty-heap)           ; h is an empty heap
(define r (heap-alloc h1 "foo")) ; stores "foo" in a new memory cell
(define h2 (eff-state r))
(define x (eff-result r)) ;
(check-equal? "foo" (heap-get h2 x)) ; checks that "foo" is in x
(define h3 (heap-put h2 x "bar")) ; stores "bar" in x
(check-equal? "bar" (heap-get h3 x)) ; checks that "bar" is in x
  
```

Handles must be unique

We want to ensure that the handles we create are **unique**, otherwise allocation could overwrite existing data, which is undesirable.

Spec

```

(define h1 empty-heap)           ; h is an empty heap
(define r1 (heap-alloc h1 "foo")) ; stores "foo" in a new memory cell
(define h2 (eff-state r1))
(define x (eff-result r1))
(define r2 (heap-alloc h2 "bar")) ; stores "foo" in a new memory cell
(define h3 (eff-state r2))
(define y (eff-result r2))
(check-not-equal? x y) ; Ensures that x ≠ y
(check-equal? "foo" (heap-get h3 x))
(check-equal? "bar" (heap-get h3 y))
  
```

How can we implement
a memory handle?

A simple heap implementation

- Let a handle be an integer
- Recall that the heap only grows (no deletions)
- A the handle matches the number of elements already present in the heap
- When the heap is empty, the first handle is 0, the second handle is 1, and so on..

Heap: A solution

- We use a hash-table to represent the heap because it has a faster random-access than a linked-list (where lookup is linear on the size of the list).
- We wrap the hash-table in a struct, and the handle (which is a number) in a struct, for better error messages. And because it helps maintaining the code.

```

(struct heap (data) #:transparent)
(define empty-heap (heap (hash)))
(struct handle (id) #:transparent)
(struct eff (state result) #:transparent)
(define (heap-alloc h v)
  (define data (heap-data h))
  (define new-id (handle (hash-count data)))
  (define new-heap (heap (hash-set data new-id v)))
  (eff new-heap new-id))
(define (heap-get h k)
  (hash-ref (heap-data h) k))
(define (heap-put h k v)
  (define data (heap-data h))
  (cond
    [(hash-has-key? data k) (heap (hash-set data k v))]
    [else (error "Unknown handle!")]))

```

Contracts

Contracts

Adding some sanity to highly dynamic code.

- Design-by-contract: idea pioneered by Bertrand Meyer and pushed in the programming language **Eiffel**, which was recognized by ACM with the Software System Award in 2006.
- Contracts are pre- and post-conditions each unit of code must satisfy (*e.g.*, a function)
- In some languages, notably F* and Dafny, pre- and post-conditions are checked at compile time!

Bibliography

Design by Contract, in *Advances in Object-Oriented Software Engineering*, eds. D. Mandrioli and B. Meyer, Prentice Hall, 1991.

Contracts in Racket

Use `define/contract` rather than `define` to test the validity of each parameter and the return value.

- The `→` operator takes a predicate for each argument and one predicate for the return value
For instance: `(→ symbol? real? string?)` declares that the first parameter is a symbol, the second parameter is numeric, and the return value is a string.

Example

```
(define/contract (f x y)
  ; Defines the contract
  (→ symbol? real? string?)
  (format "(~a, ~a)"))
```

Contracts examples

Read up on Racket's manual entry on: [data-structure contracts](#)

- `real?` for numbers
- `any/c` for any value
- `list?` for a list
- `listof number?` for a list that contains numbers
- `cons?` for a pair
- `(or/c integer? boolean?)` either an integer or a boolean
- `(and/c integer? even?)` an integer that is an even number
- `(cons/c number? string?)` a pair with a number and a string
- `(hash/c symbol? number?)` a hash-table where the keys are symbols and the keys are numbers