

CS420

Introduction to the Theory of Computation

Lecture 1: Introduction

Tiago Cogumbreiro

About the course

- **Location:** (Y01-1350) Room 1350, 1st floor, University Hall
SUBJECT TO CHANGE! We need a bigger room.
- **Schedule:** Monday, Wednesday / 4:00pm to 5:15pm

Instructor:

- **Name:** Tiago (蒂亚戈) Cogumbreiro (he/him)
- **Email:** Tiago.Cogumbreiro@umb.edu
- **Office:** (M03-0201-16) Room 0201-16, 3rd floor, McCormack
- **Office hours:** TBD



Course webpage

- **URL:** cogumbreiro.github.io/teaching/cs420/f22/
- Holds the class schedule and the syllabus

Other resources

- gitlab.com: Homework assignment PDFs
- gradescope.com: Homework/mini-test submission site
- blackboard.com: Quiz submission site
- discord.com: Office hours, communication, Q&A

Make sure you have access to each of these sites!

Breadth versus depth

- Solve quizzes and mini-tests first, because they have a **hard deadline** of 24h.
- Solve homework assignments second, because have a **soft deadline**.
You can always resubmit any homework assignment.
- Prioritize (breadth) solving more assignments/exercises over (depth) solving single assignment/exercise flawlessly.

Don't forget to fill today's quiz in Blackboard!

Course requirements

Checklist

- Install Coq 8.15 (v2022.04.0): coq.inria.fr
- Can you access Gradescope?
- Can you access Blackboard?
- Can you access #cs420 and #cs420-news in Discord? If not ask in #cs420-lounge
- Can you access Gitlab? (The invites will be rolling out until this Friday)

Heads up

- Please, **register using your UMB email address.**



Course overview

Introduction to Theory of Computation

Formal Languages

Understanding the limits of what computers and programs

- Regular languages
- Context-Free languages
- Turing-recognizable languages



A birdseye view of CS420

What are the limits of programs?

Limits of computation

- Different classes of machines
- The limits of each of these classes
- What properties each class enjoys

Limits of computation

- Different classes of machines
- The limits of each of these classes
- What properties each class enjoys

Classes of machines

<i>Class of machine</i>	<i>Applications</i>
Finite Automata	Parse regular expressions
Pushdown Automata	Parse structured data (programs)
Turing Machines	Any program

Techniques

- **State-machines**

Structure concurrency/parallelism/User Interfaces; UML diagrams

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String matching rules

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Data specification; Parsing data

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Structure concurrency/parallelism/User Interfaces; UML diagrams
- **Regular expressions** (regex)
String matching rules
- **Grammars**
Data specification; Parsing data
- **Turing machines**
Theory of computation

Techniques

- **State-machines**
Structure concurrency/parallelism/User Interfaces; UML diagrams
- **Regular expressions** (regex)
String matching rules
- **Grammars**
Data specification; Parsing data
- **Turing machines**
Theory of computation
- **Programs are proofs**
Using a programming language to write formal proofs

Some applications of formal languages

Use Case 1: DFA/NFA

Using a DFA/NFA to structure hardware usage

Use Case 1: DFA/NFA

Using a DFA/NFA to structure hardware usage

- Arduino is an open-source hardware to design **microcontrollers**
- Programming can be difficult, because it is highly concurrent
- Finite-state-machines structures the logical states of the hardware
- **Input:** a string of hardware events
- String acceptance is not interesting in this domain

Example

■ The FSM represents the logical view of a micro-controller with a light switch

Use Case 1

Declare states

```
#include "Fsm.h"  
// Connect functions to a state  
State state_light_on(on_light_on_enter, NULL, &on_light_on_exit);  
// Connect functions to a state  
State state_light_off(on_light_off_enter, NULL, &on_light_off_exit);  
// Initial state  
Fsm fsm(&state_light_off);
```

Source: platformio.org/lib/show/664/arduino-fsm

Use Case 1

Declare transitions

```
// standard arduino functions
void setup() {
  Serial.begin(9600);

  fsm.add_transition(&state_light_on, &state_light_off,
                    FLIP_LIGHT_SWITCH,
                    &on_trans_light_on_light_off);
  fsm.add_transition(&state_light_off, &state_light_on,
                    FLIP_LIGHT_SWITCH,
                    &on_trans_light_off_light_on);
}
```

Source: platformio.org/lib/show/664/arduino-fsm

Use Case 1

Code that runs on before/after states

```
// Transition callback functions  
void on_light_on_enter() {  
    Serial.println("Entering LIGHT_ON");  
}  
  
void on_light_on_exit() {  
    Serial.println("Exiting LIGHT_ON");  
}  
  
void on_light_off_enter() {  
    Serial.println("Entering LIGHT_OFF");  
}  
// ...
```

Source: platformio.org/lib/show/664/arduino-fsm



Use Case 2

Regular Expressions: Input validation

Use Case 2

Regular Expressions: Input validation

HTML includes regular expressions to perform client-side form validation.

```
<input id="uname" name="uname" type="text"  
  pattern="_([a-z]|[A-Z]|[0-9])+" minlength="4" maxlength="10">
```

- `_[a-zA-Z0-9]+`
- `[a-zA-Z0-9]` means any character between `a` and `z`, or between `A` and `Z`, or between `0` and `9`
- `R+` means repeat `R` one or more times
- In this case, the username must start with an underscore `_`, and have one or more letters/numbers
- `minlength` and `maxlength` further restrict the string's length

Use Case 3

Regular Expressions: Text manipulation

Use Case 3

Regular Expressions: Text manipulation

Programming languages include regular expressions for fast and powerful text manipulation.

Example (JS)

```
let txt1 = "Hello World!";  
let txt2 = txt1.replace(/[a-zA-Z]+/, "Bye"); // Replaces the first word by "Bye"  
console.log(txt2);  
// Bye World!
```

Use Case 4

Parsing JSON

Grammar for JSON

ANTLR is a **parser generator**.

- **Input:** a *grammar*; **Output:** a parser, and data-structures that represent the parse tree (known as a Concrete Syntax Tree)
- The HTML DOM is an example of an **Abstract** Syntax Tree

```
json: value; // initial rule
obj: '{' pair (',' pair)* '}' | '{' '}' ; // a sequence of comma-separated pairs
pair: STRING ':' value; // Example: "foo": 1
array: '[' value (',' value)* ']' | '[' ']' ; // a sequence of comma-separated values
value: STRING | NUMBER | obj | array | 'true' | 'false' | 'null';
// ...
```

Source: raw.githubusercontent.com/antlr/grammars-v4/master/json/JSON.g4

A grammar for JSON integers

```
NUMBER: '-'? INT ('.' [0-9] +)? EXP?;
```

```
fragment INT: '0' | [1-9] [0-9]*; // fragment means do not generate code for this rule
```

```
fragment EXP : [Ee] [+|-]? INT; // fragment means do not generate code for this rule
```

Source: raw.githubusercontent.com/antlr/grammars-v4/master/json/JSON.g4

A grammar for JSON

```
> ls *.java
JSONBaseListener.java JSONParser.java JSONVisitor.java
JSONBaseVisitor.java JSONLexer.java JSONListener.java
> cat JSONBaseListener.java
// Generated from ../JSON.g4 by ANTLR 4.7.2
import org.antlr.v4.runtime.tree.ParseTreeListener;

/**
 * This interface defines a complete listener for a parse tree produced by
 * {@link JSONParser}.
 */
public interface JSONListener extends ParseTreeListener {
    /**
     * Enter a parse tree produced by {@link JSONParser#json}.
     * @param ctx the parse tree
     */
    void enterJson(JSONParser.JsonContext ctx);
    /**
     * Exit a parse tree produced by {@link JSONParser#json}.
     * @param ctx the parse tree
     */
    void exitJson(JSONParser.JsonContext ctx);
}
```

CS420

- Study **algorithms** and **abstractions**
- Theoretical study of the **boundaries of computing**

Course schedule

1. Learn the Coq programming language
2. Regular languages
 - Design state machines
 - Prove properties on regular languages
3. Context-free languages
 - Design pushdown automata
 - Prove properties on regular languages
4. Turing-machines
 - Prove properties on computable and non-computable languages

On studying effectively for this content

Suggestions

- **Read the chapter before the class:**

This way we can direct the class to specific details of a chapter, rather than a more topical end-to-end description of the chapter.

- **Attempt to write the exercises before the class:**

We can guide a class to cover certain details of a difficult exercise.

- **Use the office hours and our online forum:** Coq is a unusual programming language, so you will get stuck simply because you are not familiar with the IDE or a quirk of the language

Module 1

Basics.v: Part 1

A primer on the programming language Coq

We will learn the core principles behind Coq

Enumerated type

A data type where the user specifies the various distinct values that inhabit the type.

Examples?

Enumerated type

A data type where the user specifies the various distinct values that inhabit the type.

Examples?

- boolean
- 4 suits of cards
- byte
- int32
- int64

Declare an enumerated type

```
Inductive day : Type :=  
| monday : day  
| tuesday : day  
| wednesday : day  
| thursday : day  
| friday : day  
| saturday : day  
| sunday : day.
```

- `Inductive` defines an (enumerated) type by cases.
- The type is named `day` and declared as a `: Type` (Line 1).
- Enumerated types are delimited by the assignment operator (`:=`) and a dot (`.`).
- Type `day` consists of 7 cases, each of which is tagged with the type (`day`).

Printing to the standard output

`Compute` prints the result of an expression (terminated with dot):

```
Compute monday.
```

prints

```
= tuesday  
: day
```


Interacting with the outside world

- Programming in Coq is different most popular programming paradigms
- Programming is an **interactive** development process
- The IDE is very helpful: workflow similar to using a debugger
- It's a REPL on steroids!
- `Compute` evaluates an expression, similar to `printf`

Inspecting an enumerated type

```
match d with
| monday ⇒ tuesday
| tuesday ⇒ wednesday
| wednesday ⇒ thursday
| thursday ⇒ friday
| friday ⇒ monday
| saturday ⇒ monday
| sunday ⇒ monday
end
```

Inspecting an enumerated type

```
match d with
| monday ⇒ tuesday
| tuesday ⇒ wednesday
| wednesday ⇒ thursday
| thursday ⇒ friday
| friday ⇒ monday
| saturday ⇒ monday
| sunday ⇒ monday
end
```

- `match` performs **pattern matching** on variable `d`.
- Each pattern-match is called a **branch**; the branches are delimited by keywords `with` and `end`.
- Each **branch** is prefixed by a mid-bar (`|`) (`⇒`), a pattern (eg, `monday`), an arrow (`⇒`), and a return value

Pattern matching example

Compute match monday with

```
| monday ⇒ tuesday  
| tuesday ⇒ wednesday  
| wednesday ⇒ thursday  
| thursday ⇒ friday  
| friday ⇒ monday  
| saturday ⇒ monday  
| sunday ⇒ monday
```

end.

Create a function

```
Definition next_weekday (d:day) : day :=  
  match d with  
  | monday ⇒ tuesday  
  | tuesday ⇒ wednesday  
  | wednesday ⇒ thursday  
  | thursday ⇒ friday  
  | friday ⇒ monday  
  | saturday ⇒ monday  
  | sunday ⇒ monday  
end.
```

Create a function

```
Definition next_weekday (d:day) : day :=  
  match d with  
  | monday ⇒ tuesday  
  | tuesday ⇒ wednesday  
  | wednesday ⇒ thursday  
  | thursday ⇒ friday  
  | friday ⇒ monday  
  | saturday ⇒ monday  
  | sunday ⇒ monday  
end.
```

- **Definition** is used to declare a function.
- In this case **next_weekday** has one parameter **d** of type **day** and returns (**:**) a value of type **day**.
- Between the assignment operator (**:=**) and the dot (**.**), we have the body of the function.

Example 2

```
Compute (next_weekday friday).
```

yields (Message pane)

```
= monday  
: day
```

next_weekday friday is the same as monday (after evaluation)

Your first proof

Example `test_next_weekday:`

```
next_weekday (next_weekday saturday) = tuesday.
```

Proof.

```
  simpl.      (* simplify left-hand side *)
```

```
  reflexivity. (* use reflexivity since we have tuesday = tuesday *)
```

Qed.

Your first proof

Example `test_next_weekday:`

```
next_weekday (next_weekday saturday) = tuesday.
```

Proof.

```
simpl.      (* simplify left-hand side *)
```

```
reflexivity. (* use reflexivity since we have tuesday = tuesday *)
```

Qed.

- **Example** prefixes the name of the proposition we want to prove.
- The return type (`:`) is a (logical) **proposition** stating that two values are equal (after evaluation).
- The body of function `test_next_weekday` uses the `ltac` proof language.
- The dot (`.`) after the type puts us in proof mode. (Read as "defined below".)
- This is essentially a unit test.